

# Identifying “at risk” students in first term calculus

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# Abstract

Introductory calculus courses often have a relatively high failure rate, thus acting as “gatekeeper” courses for many disciplines. Students who struggle early in the course and who have low incoming skills are known to be at a higher risk of failure. Some instructors may plan an intervention for such at risk students after a first midterm. Here we demonstrate an alternative approach. Using a multiple regression model built from student data gathered in the first month of classes, at risk students can be identified earlier in the term.

# Background

- In North America, first term calculus has a relatively high failure rate (compared with other courses).
- First term calculus acts as a “gatekeeper” course for many disciplines.
- Low incoming skills and low grades early in the course place a student at higher risk of failure.
- Some instructors will identify and reach out to at risk students after a midterm<sup>1</sup>.

<sup>1</sup> For an example of intervention, see: Deslauriers, Louis, et al. "Transforming the lowest-performing students: an intervention that worked." *Journal of College Science Teaching* 41.6 (2012): 76.

# Motivation

- Educators want to identify at risk students early in the semester when planning an intervention for such students.
- Researchers want to understand the variables that predict success in calculus.
- Administrators may want to identify at risk students early enough so they can be streamed into another calculus course.

# Correlation with grades

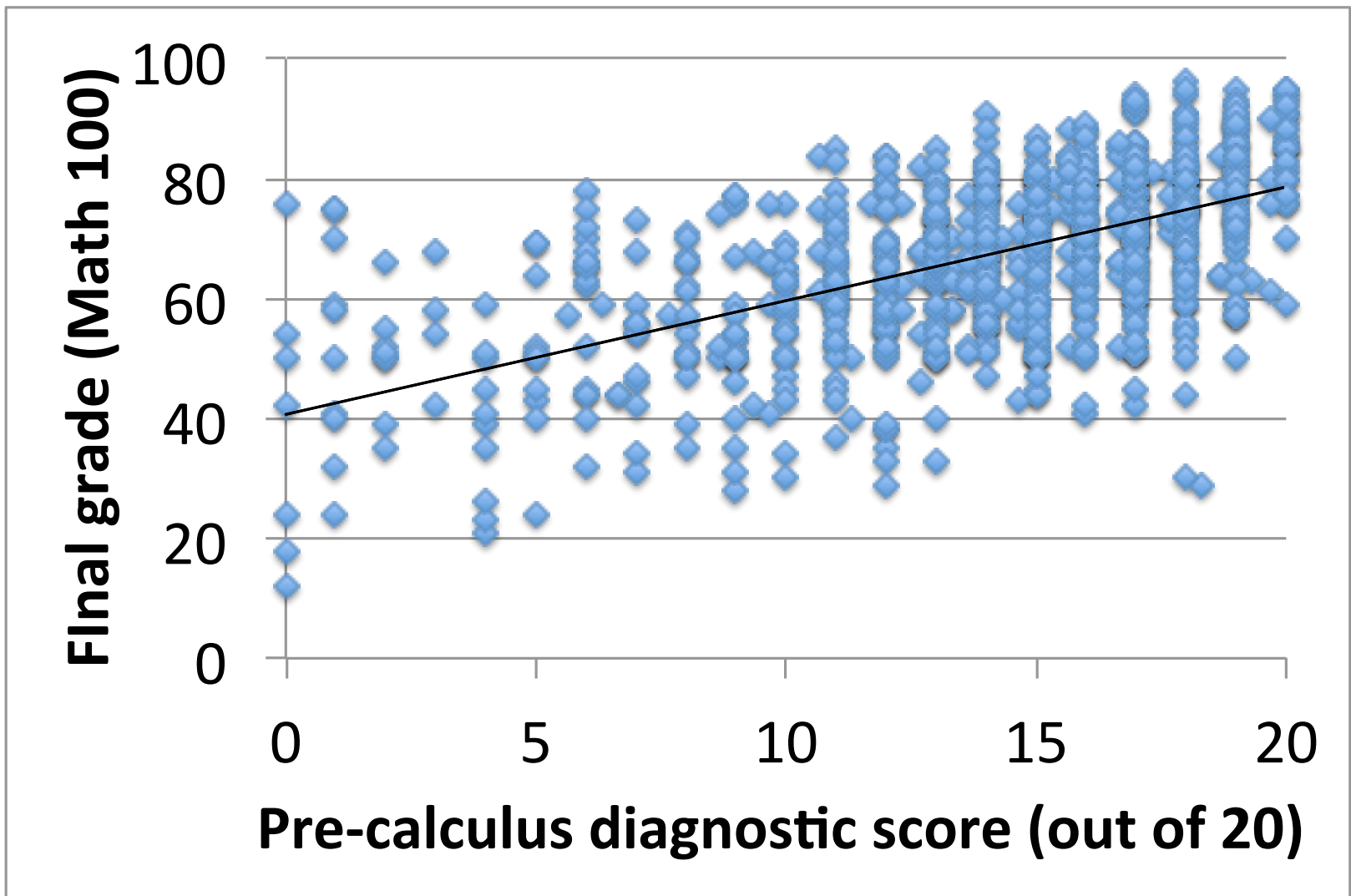
Predictor	Timeframe	Correlation with final grade (Pearson's r)	Course
Pre-calculus diagnostic (PCD)	Early September	0.57	Math 100 (N = 967)
Math attitude survey (MAPS)	Early September	0.36	Math 100 (N = 967)
First online homework (HW1)	Middle of September	0.52	Math 100 (N = 967)
First quiz (Q1)	Late September	0.58	Math 100 (N = 967)
Midterm	Mid October	0.81	Math 104 (N=789)

PCD = score on the pre-calculus diagnostic

HW1 = points per attempt for the first online homework

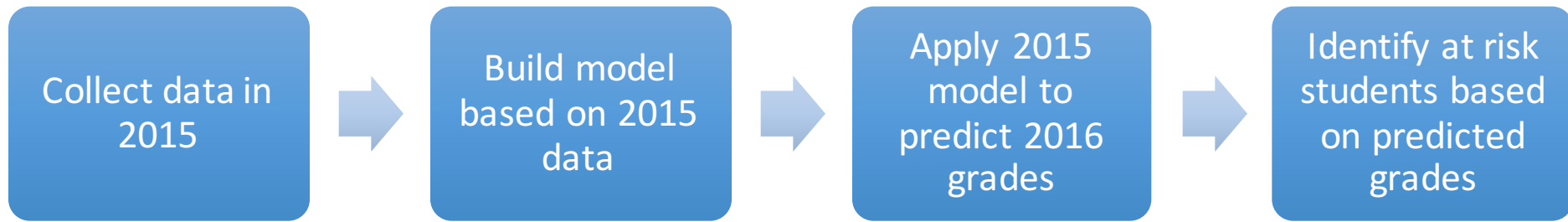
MAPS = Mathematics Attitudes and Perceptions Survey

**The Mathematics Attitudes and Perceptions Survey: an instrument to assess expert-like views and dispositions among undergraduate mathematics students**, *International Journal of Mathematical Education in Science and Technology*, 2016 Vol. 47, No. 6, 917–937



The pre-calculus diagnostic is an online homework with a suggested completion time of one hour, and students receive full credit as long as they attempt it.

# Multiple regression modeling

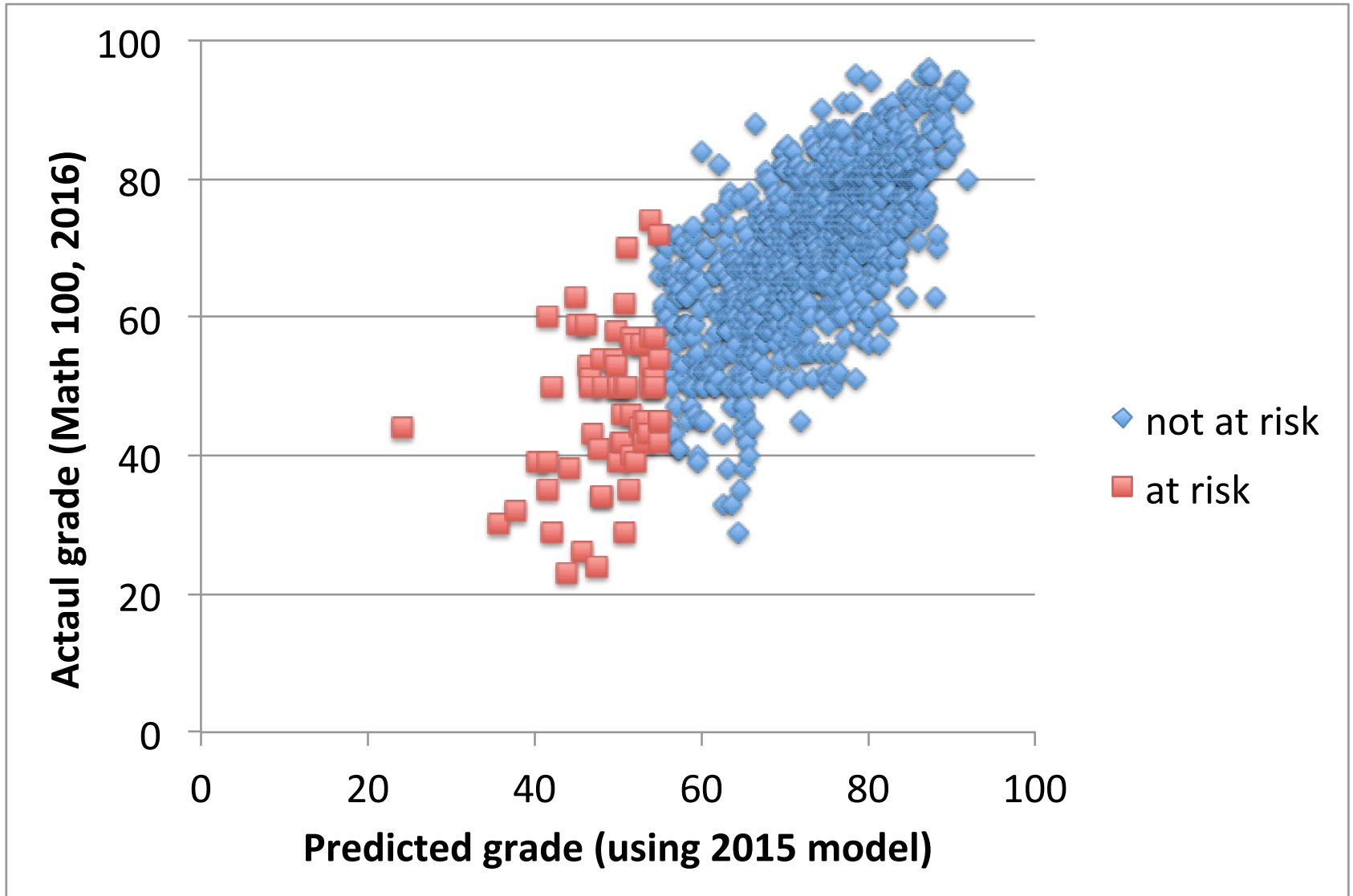


$$\text{Final grade} = \beta_0 + \beta_1(\text{PCD}) + \beta_2(\text{MAPS}) + \beta_3(\text{HW1}) + \beta_4(\text{Q1}) + \varepsilon$$

Diagram illustrating the components of the regression model:

- $\beta_1$  (PCD): pre-calculus diagnostic
- $\beta_2$  (MAPS): attitude survey
- $\beta_3$  (HW1): first homework
- $\beta_4$  (Q1): first quiz

Define a student to be “at risk” if their predicted grade is less than 55%





# Accuracy of predictions

- 50% of “at risk” students failed the course

	failed	passed	accuracy
at risk	32	32	50%
not at risk	30	873	97%

# Comparing different predictors of pass/fail (Math 100)

Predictors	Timeframe	At risk group size (predicted grade of 55% of less)	Failure rate (in the at risk group)
PCD, MAPS, HW1	Mid Sep	N = 64 (6.9% of class)	38%
First Quiz (Q1)	Late Sep	N = 64	30%
PCD, MAPS, HW1, Q1	Late Sep	N = 64	50%

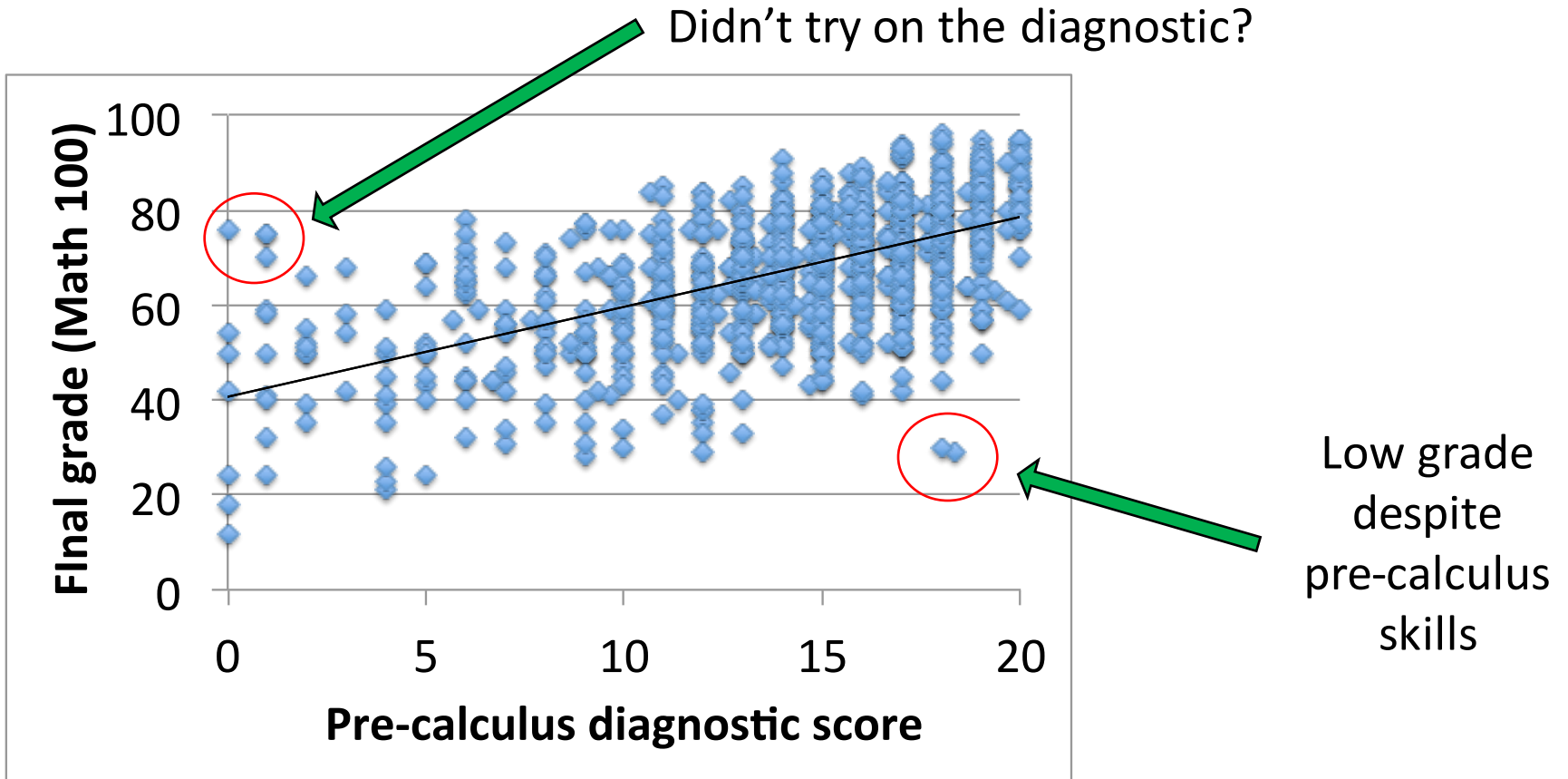
The pre-calculus diagnostic (PCD), attitude survey (MAPS) and first homework (HW1) are at least as good as the first quiz (Q1) in predicting pass/fail.

# Comparing different predictors of pass/fail (Math 100 and 104)

Predictors	Timeframe	Course	At risk group (6.7% of the class)	Failure rate (all students)	Failure rate (in the at risk group)
PCD, MAPS and HW1	Mid Sep	Math 104 (2016)	N = 52	6.6%	40%
PCD, MAPS, HW1, Q1	Late Sep	Math 100 (2016)	N = 64	6.4%	50%
Midterm	Mid Oct	Math 104 (2016)	N = 52	6.6%	65%

The midterm is a slightly better predictor of pass/fail in Math 104 than PCD/MAPS/HW1/Q1 in Math 100 (65% accuracy vs 50% accuracy).

# Outliers



# Conclusion

- Student data gathered early in the term can be used to identify at risk students.
- Regression models can be used from one year to the next.
- Current model doesn't incorporate other variables known to predict success, such as study habits.
- Predictive models will always have uncertainty; for example, they don't account for how well a student adjusts to university life.